

# A Fun Template

Senan Sekhon

October 4, 2020

## Contents

|          |                            |          |
|----------|----------------------------|----------|
| <b>1</b> | <b>Sample Chapter</b>      | <b>2</b> |
| 1.1      | Some Definitions . . . . . | 2        |
| <b>A</b> | <b>Bonus Material</b>      | <b>3</b> |

## Conventions

$\mathbb{F}$  denotes either  $\mathbb{R}$  or  $\mathbb{C}$ .

$\mathbb{N}$  denotes the set  $\{1, 2, 3, \dots\}$  of natural numbers (excluding 0).

# 1 Sample Chapter

Let's dive right in!

## 1.1 Some Definitions

**Definition 1.1.** The derivative of a function  $f : I \rightarrow \mathbb{R}$  at  $a \in I$  is given by:


$$f'(x) = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$$

You know those awesome commutative diagrams?

$$\begin{array}{ccc} A & \xrightarrow{p} & B \\ q \downarrow & & \downarrow r \\ C & \xrightarrow{s} & D \end{array}$$

The derivative has *nothing* to do with them!

**Proposition 1.2.** If  $f$  is differentiable at  $a$ , then  $f$  is continuous at  $a$ .

**Proof.** Exercise (but only because this is a template). 

The converse of Proposition 1.2 is not true in general.


**Examples.**

1.  $f(x) = |x|$
2.  $f(x) = \begin{cases} \sin(x) & x \geq 0 \\ 0 & x < 0 \end{cases}$

**Theorem 1.3.** The following statements are true:

1. First statement
2. Second statement

**Proof.**

1. Trivial.
2. Trivial. 

**Corollary 1.4.** We are both very lucky to have each other as a collaborator.

**Proof.** We simply note that:

$$\frac{1}{1} + \frac{1}{1} \gg \frac{1}{1}$$



**Remark.** This corollary is also obvious from empirical evidence.

**Lemma 1.5.**  $(a + b)^2 = a^2 + 2ab + b^2$


**Proof.** Expand the left side. 

**Remarks.**

1. It's also kind of obvious.
2. No extra points for guessing what  $(a - b)^2$  is.

**Example.**  $(2 + 4)^2 = 2^2 + 2 \cdot 2 \cdot 4 + 4^2 = 36$

**Theorem 1.6** (Pythagoras' Theorem). If  $c$  is the hypotenuse of a right triangle and  $a$  and  $b$  are the other two sides, then  $a^2 + b^2 = c^2$ .

**Proof.** Draw a picture and convince yourself. 

Pythagoras' theorem helps motivate the study of metric spaces, which you can learn about in [1].

A lot of nice integrals can be computed using the residue theorem, see [2, Section 5.2].

# A Bonus Material

The `talign` and `talign*` environments work like the `align` and `align*` environments, except they render equations in inline size. For example, `\begin{talign*}...\end{talign*}` yields:

$$\sum_{n=1}^{\infty} \frac{1}{n^2} = \frac{\pi^2}{6}$$

While `\begin{talign}...\end{talign}` yields:

$$\sum_{n=1}^{\infty} \frac{1}{n^2} = \frac{\pi^2}{6}$$

As usual, the purpose of `*` is to prevent numbering of the equation.

Some commands, like `\sumn`, can be used with or without a starting value (the default starting value is 1). For example, `$$\sumn\frac{1}{n^2}$$` yields  $\sum_{n=1}^{\infty} \frac{1}{n^2}$ , while `$$\sumn[69]\frac{1}{n^2}$$` yields  $\sum_{n=69}^{\infty} \frac{1}{n^2}$ . This can be used in inline mode as well as display mode.

# References

- [1] Senan Sekhon. “Metric and Topological Spaces”. Unpublished. 2019.
- [2] Joseph L. Taylor. *Complex Variables*. AMS, 2011. ISBN: 978-0-8218-6901-7.